

Modeling Seismic Recordings of High-Frequency Guided Infrasound on Mars

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Modelling seismic recordings of high-frequency guided infrasound on Mars

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Key Points:

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We analytically compute the dispersion relationship of guided infrasound in 1D atmospheric models from Mars and Earth; We model the ground response to guided infrasound to fit the corresponding seismic observation due to meteorite impacts on Mars; We utilize the seismic recording due to guided infrasound to constrain the subsurface structures.

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24 Abstract

NASA's InSight mission records several high-frequency (>0.5 Hz) dispersive seismic sig-25 nals on Mars. These signals are due to the acoustic-to-seismic coupling of infrasound gen-26 erated by the entry and impact of meteorites. This dispersion property is due to infra-27 sound propagating in a structured atmosphere, and we refer to this dispersive infrasound 28 as guided infrasound. We propose to model the propagation of guided infrasound and 29 the seismic coupling to the ground analytically; we use a 1D layered atmosphere on a 30 three-layer solid subsurface medium. The synthetic ground movements fit the observed 31 dispersive seismic signals well and the fitting indicates the regolith beneath InSight is 32 about 40-m in thickness. We also examine and validate the previously-published sub-33 surface models derived from InSight ambient seismic vibration data. 34

³⁵ Plain Language Summary

Under particular weather conditions, the Martian atmosphere displays a special sound-36 wave velocity profile, where the wave velocity becomes larger with increasing altitude 37 within a few hundred meters. When an infrasound signal - a low-frequency (<20 Hz) sound 38 wave inaudible to humans - propagates through such a structure, the infrasound exhibits 39 dispersion : its propagation velocity depends on its frequency. We refer to such infra-40 sound as guided infrasound. Guided infrasound can deform the ground, and have been 41 recorded by the seismometer of NASA's InSight mission on the Martian surface. We pro-42 pose to model these recordings using the physics of sound waves traveling above a com-43 pliant solid ground. We show that our modelling results can fit well the seismic record-44 ings of guided infrasound on Mars. We apply our modelling to the subsurface models 45 from a different InSight seismic observation to check if these models can explain our seis-46 mic recordings. This modelling constitutes a new tool to investigate the subsurface struc-47 ture of Mars, and is also useful for the investigation of Titan and Venus. 48

49 **1** Introduction

NASA's InSight (Interior Exploration using Seismic Investigations, Geodesy and 50 Heat Transport) mission landed on the Martian surface in November 2018 and has since 51 been conducting geophysical and meteorological observation (Banerdt et al., 2020). To 52 achieve its objectives, InSight is equipped with a Very Broad Band (VBB) and a Short 53 Period (SP) seismometer, which together constitute the SEIS (Seismic Experiment for 54 Internal Structure) instrument (Lognonné et al., 2019). SEIS is operated in combina-55 tion with a weather station, Auxiliary Payload Sensor Suite (APSS) including an atmo-56 spheric pressure sensor and wind and temperature sensors, to perform meteorological ob-57 servation (Banfield et al., 2019). Due to power issues appearing in the second Martian 58 year of the mission, SP and APSS have become temporarily unavailable, and VBB has 59 been kept on most of the time. Thus only the VBB seismic data is available for analyz-60 ing the seismic events in this study. 61

The ground motion recorded by InSight originates from different types of sources, 62 most of which are marsquakes (e.g. Giardini et al., 2020) or atmospheric seismic events 63 like pressure drops (e.g. Lognonné et al., 2020). The recent seismic recordings provides 64 a new type of seismic events, a dispersive wave train following a typical very-high-frequency 65 (VF) marsquake (Clinton et al., 2021), where a dispersive wave train means that the wave 66 velocity, also arrival time, depends on frequency. This wave train appears about a few 67 hundred of seconds after the P arrivals, such as in events S0793a, S0981c, and S0986c. 68 Based on analysis of seismic arrival times and satellite imagery, Garcia et al. (2022) demon-69 strate that these events are generated by meteorite impacts on the Martian surface (Fig-70 ure 1). Thus, the high-frequency seismic energy arriving before the dispersive waves is 71 due to the meteorite cratering process (Figure 2a). 72

The meteors not only generate the craters but also interact with the Martian at-73 mosphere during entry and impacting, which generates infrasound, i.e. acoustic waves 74 with a frequency lower than 20 Hz (Figure 2). The infrasound propagation medium - the 75 atmosphere - can exhibit a particular structure, where the infrasound propagation ve-76 locity is smaller near the ground surface than at higher altitudes (about a few hundred 77 meters). In such structures, multiple infrasound propagation paths interfere with each 78 other, and the interference generates dispersion (Herrin et al., 2006; Negraru & Herrin, 79 2009), similar to the mechanism of Love waves in seismology (e.g. Aki & Richards, 2002). 80 This infrasound velocity model in Earth is referred to as nocturnal boundary layer in acoustic-81 wave literature (e.g. Waxler, 2004), since such a model is usually generated when the 82 temperature on the ground surface decreases at night, leading to a cooling of the lower 83 atmosphere. This phenomenon is common on Mars due to the quick cooling down of the 84 Martian surface at night and/or high-altitude winds (e.g. Garcia et al., 2017). In this 85 study, we refer to this atmospheric structure as a waveguide, and we refer to the inter-86 fered infrasound waves as guided infrasound. Guided infrasound can be simulated nu-87 merically by solving the acoustic wave equations (e.g. Garcia et al., 2017; Martire et al., 88 2020). This numerical simulation approach can address complicated atmospheric mod-89 els like a laterally heterogeneous atmosphere with winds, but is computationally expen-90 sive. One can also model the guided infrasound waveform analytically by calculating the 91 phase/group velocity (i.e. dispersion) within a laterally-homogeneous two-layer atmo-92 spheric model (Negraru & Herrin, 2009). This analytical approach is much faster and 93 less computationally expensive than the numerical simulation, and is therefore well suited 94 to explore different atmospheric parameters and their associated guided infrasound. How-95 ever, former studies remain limited to two-layer atmospheric models. In this study, we 96 extend this analytical approach to a multiple-layer model using the propagation matrix 97 method described in seismic surface-wave studies (e.g. Aki & Richards, 2002). Note that 98 in this study we focus on the high-frequency guided infrasound, while on Earth, the lowfrequency (<0.02 Hz) guided infrasound also exists (e.g. Pekeris, 1948; Press & Harkrider, 100 1962; Harkrider, 1964). 101

We use the VBB seismic data (InSight Mars SEIS Data Service, 2019a, 2019b) to 102 study guided infrasound observed on Mars, because infrasound propagates with atmo-103 spheric perturbations and the perturbations deform the ground (e.g. Sorrells, 1971; Tan-104 imoto & Wang, 2019). One has observed this type of coupling due to atmospheric pres-105 sure drops through seismic recordings on both Earth and Mars (e.g. Lorenz et al., 2015; 106 Lognonné et al., 2020; Kenda et al., 2020). Furthermore one also observes infrasound de-107 forming Earth's ground surface due to acoustic sources such as volcanic activities (e.g. 108 Ichihara et al., 2012), meteors (e.g. Edwards et al., 2008), and ground surface explosions 109 (e.g. Gibbons et al., 2007; Schneider et al., 2018). Conversion of an atmospheric pres-110 sure perturbation into ground deformation is called compliance, and the intensity of com-111 112 pliance is determined by the subsurface structure and the propagation velocity of the perturbation (e.g. Ewing et al., 1957; Sorrells et al., 1971; Ben-Menahem & Singh, 2012). 113 We detail computation of compliance in Section 3. 114

We propose to analytically model the seismic recordings due to guided infrasound, 115 and we refer to the recordings as chirps. We demonstrate computation of the guided in-116 frasound phase and group velocities in multiple-layer atmospheric models (Section 2). 117 We then introduce the compliance and our subsurface velocity model (Section 3). We 118 combine the guided infrasound and the compliance to generate a synthetic chirp; we use 119 the synthetic chirp to fit the observed ones (Section 4). We finally discuss the implica-120 tion of our modelling to the previously-published subsurface models and the infrasound 121 propagation in the Martian atmosphere (Section 5). Our research can aid the investi-122 gation of atmospheric and subsurface properties, not only on Mars and Earth but also 123 on other bodies with atmosphere such as Titan and Venus. 124



Figure 1. Topography map (Smith et al., 2001) of the Martian surface around InSight and three impact locations (S0793a, S0981c, and S0986c). The impact locations are constrained by CTX images (Garcia et al., 2022).

¹²⁵ 2 Modelling Guided infrasound

126 **2.1** Theory

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We solve the dispersion of the guided infrasound in a multiple-layer atmospheric model theoretically. We present an example of the Martian guided infrasound in this section and an Earth example in Appendix A. We assume the atmosphere to be adiabatic, which leads to the following 2D governing equations:

 $-\partial_z p = \rho D_t v_z,\tag{1}$

$$-\partial_x p = \rho D_t v_x,\tag{2}$$

$$-D_t p = K(\partial_z v_z + \partial_x v_x), \tag{3}$$

where ∂_z denotes the partial derivative with respect to altitude (z), p is the atmospheric pressure perturbation conveyed by the infrasound wave, ρ is the air density, and K is the incompressibility; v_z and v_x are the particle velocities in the vertical and horizontal directions, respectively. D_t denotes the material derivative with respect to time. Indeed, the advection of momentum cannot be ignored here, as the horizontal wind velocity (w_x) can reach up to about 15 m/s on the Martian surface. The effect of w_x is made explicit by rewriting the above equations as:

$$-\partial_z p = \rho(\partial_t + w_x \partial_x) v_z, \tag{4}$$

$$-\partial_x p = \rho(\partial_t + w_x \partial_x) v_x, \tag{5}$$

$$-(\partial_t + w_x \partial_x)p = K(\partial_z v_z + \partial_x v_x).$$
(6)

Since in the three impact events, the cross winds deviate the infrasound propagation direction by less than 5 deg (Garcia et al., 2022), we neglect the cross wind effect and project the total wind speed to the guided infrasound propagation direction to achieve w_x (Table S1, S2, and S3). Besides the above equations, a set of boundary conditions is also needed. We adopt a rigid ground surface, such as:

$$v_z(z=0) = 0.$$
 (7)



Figure 2. Illustration of the S0986c event (a) and data (b, c). (a) The meteor of the S0986c impact interacts with the Martian subsurface and atmosphere, generating seismic waves (from 0 to about 200 s in (b) and infrasound (after 200 s in b), respectively. The vertical scales of the atmosphere and the subsurface are in hundred meter and kilometer, respectively. (b) The S0986c VBB vertical-component data. The data is bandpass filtered between 0.1 and 8 Hz. The insert shows a zoom of the chirp in the blue box. (c) Spectrogram of the data in (b). The blue box indicates the chirp spectrogram. The red box indicates other arrivals of infrasound energy. The time axis is in Coordinated Universal Time (UTC).

Note that one may choose an elastic ground-surface boundary condition and then the
right hand side of the above equation would not be zero anymore (e.g. Waxler, 2002).
We justify our rigid boundary condition in Section 5.3. We use the radiation boundary
condition for the top boundary. The 2D geometry assumed here is a good approximation for a real 3D geometry only if the cross-wind can be neglected (e.g. Nijs & Wapenaar, 1992). Other second-order factors are not considered here, such as the effect of static
pressure or gravity (e.g. Pierce, 1990).

We compute the guided infrasound phase velocities by solving the above equations (Equation 4, 5 and 6) and the boundary conditions (e.g. Equation 7). One can adopt normal mode expansion to solve the equations, and Assink (2012) present a complete review of this approach mathematically. However, this approach is not designed specifically for guided infrasound and is built on an elastic boundary condition, instead of our rigid one (Equation 7). Thus, we propose a simpler method. We assume that guided infrasound propagates horizontally as a plane wave:

$$p = P(\omega, z) \exp(i(\omega t - kx)), \tag{8}$$

$$v_z = V_z(\omega, z) \exp(i(\omega t - kx)), \tag{9}$$

$$v_x = V_x(\omega, z) \exp(i(\omega t - kx)), \tag{10}$$

where ω is the angular frequency, z is altitude, t is the propagation time, k is the hor-

izontal wavenumber, and x is the propagation distance. Note that ω/k gives the phase

velocity. Based on Equation 5, 8, and 10, we notice that

$$V_x = \frac{kP}{\rho(\omega - w_x k)}.$$
(11)

¹⁷⁰ We then rewrite the governing equations in a matrix form as

$$\partial_{z} \begin{bmatrix} P \\ V_{z} \end{bmatrix} = \begin{bmatrix} 0 & -i(\omega - w_{x}k)\rho \\ -i\omega/\alpha^{2}/\rho + iw_{x}k/\rho/\alpha^{2} + ik^{2}/(\omega - w_{x}k)/\rho & 0 \end{bmatrix} \begin{bmatrix} P \\ V_{z} \end{bmatrix}, \quad (12)$$

where α is the infrasound velocity, where $\alpha^2 = K/\rho$. Note that Press and Harkrider (1962) and Nijs and Wapenaar (1990) have achieved similar equations as Equation 12. Press and Harkrider (1962) study the low-frequency (<0.02 Hz) guided infrasound considering gravity, and Nijs and Wapenaar (1990) study acoustic wave propagation and do not consider the guided infrasound.

We use the propagation matrix method (e.g. Aki & Richards, 2002) to solve Equation 12. This equation is in the form of $\partial_z \vec{f} = \mathbf{A}\vec{f}$, where \vec{f} is normally referred to as eigenfunctions and \vec{f} here contains P and V_z . The propagation matrix is defined as $\mathbf{M}(z, z') =$ $\exp[(z - z')\mathbf{A}]$ between two depths, z and z'. We use \mathbf{M} to calculate the eigenfunctions at z from z' as

$$\vec{f}(z) = \mathbf{M}(z, z')\vec{f}(z'). \tag{13}$$

¹⁸¹ We observe that Equation 13 intuitively satisfies Equation 12. For a 1D atmospheric model, ¹⁸² with a right phase velocity (i.e. ω/k) at frequency ω , we can calculate the eigenfunctions ¹⁸³ at all altitudes, and the eigenfunction values on the ground surface would satisfy the bound-¹⁸⁴ ary condition (Equation 7). The computation is detailed in Section S1. Based on the phase ¹⁸⁵ velocity, we can also compute the group velocity as the variation of ω over the variation ¹⁸⁶ of k (e.g. Aki & Richards, 2002).

¹⁸⁷ 2.2 S0986c guided infrasound

We use an atmospheric model of Mars to illustrate the eigenfunctions and the group velocities of the S0986c guided infrasound (Figure 3). We adopt the atmospheric model parameters (acoustic-wave velocity, wind speed, air density, and altitude) from the Mars

Climate Database (MCD, Millour et al., 2018). We project the wind speed along the back-191 azimuth of SEIS with regards to the S0986c impact location (Figure 1 and Table S3); 192 the cross wind of this event atmospheric model does not obviously affect the infrasound 193 propagating from the impact location to InSight (Garcia et al., 2022). Note that MCD 194 models the Martian climate at a global scale and could be biased at local scale like our 195 cases. Thus we modify the acoustic-wave velocity by fitting the synthetic group veloc-196 ity to the measurement from the chirp (Garcia et al., 2022). We add (subtract) a con-197 stant value to (from) acoustic-wave velocities at all altitudes, which moves the whole syn-198 thetic group-velocity curve up (down) but does not change the synthetic group-velocity 199 shape (Figure 3c). The sum of the projected wind speed and the modified acoustic-wave 200 velocity is called the effective velocity (Figure 3a). The effective velocity of this event 201 increases gradually with altitude until about 500 m and then decreases slightly. We dis-202 cretize the wind speed and the acoustic-wave velocity to form a 1D layered model, and 203 then compute the phase velocity (Figure 3c) and the atmospheric pressure eigenfunc-204 tions (P, Figure 3b). The pressure eigenfunctions are real valued and maximal on the 205 ground surface. We also observe that a high-frequency (3 Hz) eigenfunction decays faster 206 than a low frequency one (1 Hz) with increasing altitude. The pressure eigenfunction rep-207 resents the amplitudes (P in Equation 8) of the guided infrasound at different altitudes. 208 For example, in this case, we would receive a lower-amplitude guided infrasound with 209 an atmospheric-pressure sensor at 500 m altitude (like a balloon) compared to a sensor 210 on the ground surface. The eigenfunctions also represent the excitation amplitude of the 211 guided infrasound due to the source-receiver reciprocity (e.g. Landau & Lifshitz, 2013; 212 Aki & Richards, 2002). Therefore an infrasound source at 500 m would generate weaker 213 infrasound compared to a source on the ground surface. We use the phase velocity later 214 in our computation of compliance (Section 3) and our chirp modelling (Section 4). 215

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2.3 Higher-mode guided infrasound

We present the fundamental-mode guided infrasound in the above. The fundamentalmode represents the lowest-phase-velocity root in solving Equation 12 at each frequency, while the higher-velocity roots may also exist (Figure S1) and are referred to as the higher modes. The fundamental mode usually dominates guided infrasound in observations (e.g. Negraru & Herrin, 2009). Thus in the group-velocity measurement of S0981c and S0986c, we only observe the trends corresponding to the fundamental modes (Figure S1b and S1c).

We also demonstrate the domination of the fundamental-mode by computing the 224 contribution of both the fundamental and higher modes to the pressure on the ground 225 surface as $P^2(z=0)/\int P^2(z)dz$. The pressure eigenfunction (P) is real valued if the cor-226 responding mode is a trapped mode (e.g. Lognonné et al., 1998; Chakravarthy, 2008). 227 However, at some frequencies, the eigenfunctions become complex valued, and the imag-228 inary parts represent the energy leakage of the guided infrasound to the top halfspace 229 (e.g. Press & Harkrider, 1962; Radovich & De Bremaecker, 1974). Thus we only use the 230 real part of the eigenfunctions on the ground surface in computing the contributions (Fig-231 ure S1). We observe that for S0981c and S0986c, the contribution of the fundamental 232 modes are at least one magnitude (a factor of ten) larger than the higher modes at each 233 frequency. However, for S0793a, the 1st-higher mode contributes more than the funda-234 mental mode. We investigate this phenomenon in detail in Section 5.2. 235

²³⁶ 3 Compliance: acoustic-to-seismic conversion

Atmospheric pressure perturbations, e.g. caused by wind or infrasound, can deform
the ground at shallow depths on planets with atmosphere (e.g. Sorrells, 1971; Ben-Menahem
& Singh, 2012), like the atmospheric noise recorded by SEIS on Mars (Lognonné et al.,
2020; Garcia et al., 2020; Stutzmann et al., 2021). Furthermore, when the infrasound hor-



Figure 3. The infrasound velocity model (a), eigenfunctions (b), dispersion (c) and compliance (d) for S0986c. (a) We compute the infrasound velocity and the wind speeds from MCD for S0986c (Millour et al., 2018) and subtract 4 m/s from the velocity at all altitudes (red dashed line). The black line represents our 1D layered model. (b) Two different-frequency pressure eigenfunctions are normalized by each maximum value for visualization. (c) The gray background is the group-velocity measurement of the S0986c chirp (Garcia et al., 2022). (d) The vertical (black) and horizontal (blue) compliance is based on the phase velocity (c) and a subsurface velocity model (Table 1). The infrasound attenuation (blue) is from Bass and Chambers (2001) for 200 K temperature.

izontal apparent velocity is equal to the seismic-wave velocities of the subsurface, the in-241 frasound would convert into seismic waves (e.g. Ewing et al., 1957; Langston, 2004). To 242 summarize these different types of acoustic-to-seismic coupling, Edwards et al. (2008) 243 list the possible conversion scenarios for homogeneous and isotropic elastic subsurface 244 media. Note that in this study, we mainly focus on the so-called normal coupling, i.e. 245 atmospheric pressure perturbations deforming the ground surface without generating seis-246 mic waves, but the following theory remains applicable to all the scenarios mentioned 247 above. Due to the frequency band we use (here from 0.5 to about 2 Hz), we only con-248 sider the compliance in this study and ignore other effects like tilt (Garcia et al., 2020). 249

Compliance is the amplitude relationship between the pressure perturbation and 250 the ground deformation. Compliance is determined by the subsurface structure and the 251 propagation velocity of the pressure perturbation in the atmosphere overlaying the sub-252 surface (e.g. Sorrells, 1971; Ewing et al., 1957; Ben-Menahem & Singh, 2012), based on 253 the assumption that the perturbation propagates like a plane wave. Note that the plane-254 wave assumption even holds for a complex pressure wavefield, since the complex wave-255 field can be decomposed into plane waves (e.g. Kenda et al., 2017). In the subsurface 256 media, the ground motion and normal stress (τ_{zz}) are defined as: 257

$$u_z(z) = U_z(\omega, z) \exp(i(\omega t - kx)), \tag{14}$$

$$u_x(z) = iU_x(\omega, z) \exp(i(\omega t - kx)), \tag{15}$$

$$\tau_{zz}(z) = T_{zz}(\omega, z) \exp(i(\omega t - kx)), \tag{16}$$

where u_z and u_x are the vertical and horizontal ground velocities, respectively; ω , k, t, 262 and x are the same as in guided infrasound (Equation 8) while z here is the depth be-263 low the surface. The i in front of U_x in Equation 15 represents the $\pi/2$ phase shift be-264 tween the horizontal and vertical components of the ground motion (e.g. Sorrells, 1971). 265 We then write compliance as the amplitude ratio of the vertical (horizontal) ground ve-266 locities over the atmospheric pressure perturbation: 267

$$C_z = \frac{u_z(z=0)}{(z=0)} = \frac{U_z(\omega, z=0)}{D(z=0)} = -\frac{U_z(\omega, z=0)}{D(z=0)},$$
(17)

$$C_{z} = p(z=0) - P(\omega, z=0) - T_{zz}(\omega, z=0),$$

$$C_{x} = \frac{u_{x}(z=0)}{(z=0)} = \frac{iU_{x}(\omega, z=0)}{P(\omega, z=0)} = -\frac{iU_{x}(\omega, z=0)}{T_{zz}(\omega, z=0)},$$
(18)

$$C_x = \frac{u_x(z=0)}{p(z=0)} = \frac{iU_x(\omega, z=0)}{P(\omega, z=0)} = -\frac{iU_x(\omega, z=0)}{T_{zz}(\omega, z=0)},$$

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where $T_{zz}(z = 0) = -P(z = 0)$ (Equations 8 and 16) implies the continuity of nor-271 mal stress on the ground surface. The minus sign is due to the different sign conventions 272 between atmospheric studies and seismology. In acoustics wave studies (Section 2), the 273 atmospheric pressure compressing the ground surface is defined as being positive, i.e. ex-274 erting a force in the vertically downward direction on the ground surface. However in 275 seismology, a positive normal stress acting on a surface corresponds to a traction in the 276 outward normal direction, i.e. the vertically upward direction on the flat ground surface. 277 Note that here we refer to the vertical ground velocity as u_z , not to be mistaken with 278 the vertical particle velocity in the atmosphere, i.e. v_z in Section 2. 279

To calculate the compliance values, we use the equation of motion and Hooke's law 280 in 1D media (e.g. Aki & Richards, 2002, Chapter 7.2) and the zero-shear-stress bound-281 ary condition on the ground surface: 282

$$\tau_{zx} = 0. \tag{19}$$

Our computation is similar to Tanimoto and Wang (2019) where one does not assume 284 the propagation velocity of pressure perturbation much slower than the shear-wave ve-285 locity of the subsurface medium. In this study, we use a three-layer velocity model sim-286 plified from the shallow (<100 m) geological structure under InSight (e.g. Warner et al., 287 2022). The first layer is made of thin soft regolith, as suggested by the analyses of the 288 Martian atmospheric pressure drops (Kenda et al., 2020; Onodera, 2022) and of the ham-289 merings of InSight's Heat Flow and Physical Properties (HP³) instrument (Lognonné 290

Table 1. Parameters for a three-layer subsurface. The first two layers are regolith. In the first two layers, we calculate V_P from V_S based on the 0.22 Poisson's ratio (e.g. Morgan et al., 2018); we compute the density applying Gardner's empirical relationship (Gardner et al., 1974) to V_P .

Layer number	$V_P(m/s)$	$V_S(m/s)$	Density (kg/m^3)	Thickness (m)
1	117	70	1019	0.6
2	384	230	1372	40
3	3000	1700	2760	∞

et al., 2020). This surface layer is interpreted as fine-sand-dominated regolith. The sec-291 ond layer possesses a higher wave velocity than the first layer and represents coarse re-292 golith (e.g. Warner et al., 2017). The third layer (i.e. halfspace) corresponds to the bedrock, 293 composed of fractured basalt (e.g. Morgan et al., 2018). We use this three-layer model 294 to compute compliance in the waveform modelling (Section 4). We achieve the param-295 eters of the second layer through a waveform fitting in Section 4. Note that this model 296 is simple and may not reflect the complexity of the real subsurface under InSight. We 297 discuss possible improvement to this model in Section 5.4. 298

We notice that the difference of vertical velocities on the ground surface between 299 the atmosphere and the subsurface give rise to a contradiction. In Section 2, we assume 300 the vertical atmosphere velocity on the ground surface to be zero (Equation 7). The par-301 ticle velocity should be continuous at the fluid-solid (i.e. atmosphere-ground) interface, 302 and thus $u_z(z=0)=0$. However, a nontrivial compliance requires the vertical move-303 ments of the ground surface to be non-zero, i.e. $u_z(z=0) \neq 0$. We address this con-304 tradiction in Section 5.3. Note that such contradiction does not exist for the horizon-305 tal velocities, since the horizontal velocity of the ground surface is not necessarily con-306 tinuous with the horizontal atmospheric particle velocity. 307

³⁰⁸ 4 Waveform Forward modelling

We model synthetic chirp, the seismic recording due to guided infrasound, by combining the theories of guided infrasound (Section 2) and compliance (Section 3). The farfield synthetic ground velocity recordings of chirps (u) in the time domain are written as:

$$u_z = \mathscr{F}^{-1} \left[S(\omega) \exp\left(-ikx - ax\right) \frac{\exp\left(-i\pi/4\right)}{\sqrt{kx\pi/2}} \frac{P^2(\omega, 0)}{\int P^2(\omega, z) dz} C_z(\omega) \right],\tag{20}$$

$$u_x = \mathscr{F}^{-1} \left[S(\omega) \exp\left(-ikx - ax\right) \frac{\exp\left(-i\pi/4\right)}{\sqrt{kx\pi/2}} \frac{P^2(\omega, 0)}{\int P^2(\omega, z) dz} C_x(\omega) \right],\tag{21}$$

where \mathscr{F}^{-1} denotes the inverse Fourier transform, and S is the source time function of 313 guided infrasound. k is guided infrasound horizontal wavenumber and is from our cal-314 culation of the guided infrasound phase velocity (Section 2). x is infrasound travelling 315 distance from the infrasound source to InSight (Table 2). a is the intrinsic attenuation 316 coefficient for infrasound (Figure 2d and Bass & Chambers, 2001). exp $(-i\pi/4)/\sqrt{kx\pi/2}$ 317 is from the far-field approximation of a 3D cylindrical wave (e.g. Landau & Lifshitz, 2013). 318 $P^2(\omega,0)/\int P^2(\omega,z)dz$ is the normalized pressure eigenfunction, representing the source 319 excitation and sensor receiving on the ground surface. C_z (C_x) is the vertical (horizon-320 tal) compliance (Section 3). We use the three-layer subsurface velocity model (Table 1) 321 in computing the compliance, where the model is from simplification of the shallow ge-322 ological structure under InSight (e.g. Warner et al., 2022). We benchmark our modelling 323

Event	Estimated origin time (UTC)	Distance (km)	Backazimuth (deg)
S0793a	2021-2-18T19:36:06	91.1	274.2
S0981c S0986c	2021-8-31T04:3:13 2021-9-5T05:23:44	$243.6 \\ 85.1$	179.2 111.6

Table 2. The origin time estimates and the geometry information of the three impact events relative to InSight (Garcia et al., 2022).

approach against a numerical simulation software, SPECFEM2D-DG (Martire et al., 2020),
 in Appendix B.

We use the synthetic chirp to fit the one due to an impact. We assume that the 326 infrasound source generated by the meteor impacting is impulsive and thus the source 327 time function (S in Equation 20 and 21) is a delta function in the time domain and a 328 constant in the frequency domain. The source location is at the same location as the im-329 pact crater. Note that the source time function generated by a meteorite interacting with 330 the Martian atmosphere in the impact is worth further investigation, but is beyond the 331 scope of this study. Since the infrasound source is on the ground surface, we mainly ob-332 serve the guided infrasound on InSight (Garcia et al., 2022). 333

We use the observed chirps from two events (S0981c and S0986c) in the fitting. For 334 each event, we use the origin time estimate from the seismic arrival time (Table 2, Gar-335 cia et al., 2022). The infrasound source is at the crater associated to the events. The satel-336 lite images of these craters provide the exact distances and backazimuth (Table 2). Note 337 that these distances and backazimuth are matched closely by analysis of the two seis-338 mic recordings, e.g. body-wave arrival times and chirp polarization (Garcia et al., 2022). 339 We focus on the vertical and radial components, where the radial direction is parallel 340 to a great path from the seismic source to InSight. For the seismic recordings of the two 341 events, we rotate the north and east components to the radial direction based on the back-342 azimuth (Table 2). We apply a bandpass filter to the components of each chirp. For each 343 chirp, we choose the filter band to have high signal-to-noise ratios and to avoid spectral 344 anomaly like the sharp amplitude drop at 2.3 Hz in the S0986c vertical component (Fig-345 ure 4). In the following waveform fitting, we refer to the filtered data as real data. A chirp 346 also exists in the S0793a recording. However, that chirp displays complex properties (e.g. 347 higher-mode), which deserve to be discussed independently (Section 5.2). 348

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We compute the misfit between the synthetic and real chirps like

$$\chi = \sum_{j} \frac{1}{T} \int_{T} \left| \frac{u_z(s_j)}{\max(|u_z(s_j)|)} - \frac{u_z^o(s_j)}{\max(|u_z^o(s_j)|)} \right| + \left| \frac{u_x(s_j)}{\max(|u_z(s_j)|)} - \frac{u_x^o(s_j)}{\max(|u_z^o(s_j)|)} \right| dt \quad (22)$$

where s_i represents each event; the integral is done in the time window of each chirp (Fig-350 ure 4) and T is the time window length for each chirp. We fix the first and third layers 351 of the model, and only vary the V_S and the layer thickness of the second layer to find 352 the misfit minimum (Figure 5). The S0981c misfit mainly varies with the layer thickness 353 but does not change obviously with V_S when the thickness is less than 40 m (Figure 5a). 354 The S0986c misfit presents a sloping area (Figure 5b) where the different combinations 355 of the two parameters give similar misfits, which is known as trade-off in the geophys-356 ical inverse theory. In the total misfit of the two events (Figure 5c), the V_S and the layer 357 thickness from the minimum provide good waveform fitting between the synthetic and 358 real chirps (Figure 4). We discuss this model in the geological context in Section 5.1. 359



Figure 4. The vertical- and radial-component amplitude spectra of the chirps and noise (a,b) and the waveform fitting of the chirps in the time domain (c,d,e,f). The black and blue waveforms are the observed data and the red waveforms are the synthetic data. For each event, the signal spectra are from the time window used in the second and third rows, and the noise spectra are from the same-window-length recordings before the chirp. The gray areas indicate the frequency bands used in filtering the chirps, from 0.55 to 0.9 Hz for S0981c and from 0.5 to 2.2 Hz for S0986c.



Figure 5. The misfit between the synthetic and observed chirp signals varies with the V_S and the thickness of the second subsurface layer (Table 1). The gray color indicates the misfit value. The red triangles correspond to the least misfit of the two events, while the empty triangle (a,b) corresponds to the least misfit of each event. The empty areas are the parameter combinations where the misfit values are larger than the color bar maximum or an air-coupled Rayleigh wave is excited.

360 5 Discussion

Our analytical waveform modelling aid us validating the Martian subsurface models from other observations (Section 5.1). By combining our modelling and the Martian atmospheric model, we provide an explanation for the S0793a seismic observation (Section 5.2). We also discuss how to improve our modelling in the future (Section 5.3 and 5.4).

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5.1 Implication for the subsurface structure

Our waveform fitting provides a velocity model where the V_S increases with depth 366 (Table 1). In this model, the first layer is interpreted as fine-sand-dominated regolith (e.g. 367 Grott et al., 2021). Compared to the V_S of the first layer, the second-layer V_S is larger 368 and thus corresponds well to a coarse regolith where pebbles exist. The second layer is 369 of 40-m thickness, close to the estimate of the maximum surficial regolith thickness around 370 InSight; however, the geological model beneath the InSight indicates that this coarse re-371 golith layer is interrupted by a basalt layer (e.g. Warner et al., 2022). Note that the ge-372 ological model is built by considering the velocity models from the horizontal-to-vertical 373 (H/V) ratio measurement of the InSight ambient seismic vibration (Hobiger et al., 2021); 374 we refer to the velocity models as the H/V models. To further investigate this layer thick-375 ness contradiction, we check how the synthetic waveforms from the H/V models fit the 376 chirps. 377

We choose one of the H/V models (Figure 6a), which is close to the geological model, 378 and then generate the synthetic waveforms (Figure 6b-e) following our computation in 379 Section 4. We notice that for S0981c, the radial-component waveform of the H/V model 380 possesses larger amplitudes than the observed chirp; for S0986c, the radial component 381 from the H/V model does not fit the observed waveform around 5:29:50. The total mis-382 fit of the H/V model (Equation 22) is 0.44, 15% larger than the total misfit of our three-383 layer model, 0.40. Thus our model provides a better waveform fitting to the chirps than 384 the H/V model. We repeat the above process with the other three H/V models (Figure S2,S3,S4). 385 We notice that all the three models provides smaller radial-component amplitudes com-386 pared to the real chirps. 387



Figure 6. Comparison of the chirp waveform fitting between the H/V and the 3-layer models. The H/V model (blue) is the weakly-constrained maximum a posteriori estimation from Hobiger et al. (2021) and provides the blue dashed waveforms (b,c,d,e). The black and red waveforms (b,c,d,e) are the same observed and synthetic chirps from Figure 4, respectively.

The synthetic waveforms from the H/V models fit the vertical component of the 388 recordings (Figure 6,S2,S3,S4). Thus the H/V models does not contradict with the chirp 389 observation. Meanwhile, this waveform fitting difference between the H/V and our mod-390 els could be due to the different sensitivities of the H/V ratio and the compliance to a 391 same elastic property (e.g. Maupin, 2017; Kenda et al., 2020). Therefore, even through 392 our model explain the chirps better than the H/V models, we cannot determine if our 393 model is closer to the real subsurface than the H/V models. In order to achieve an ac-394 curate subsurface model, we need to incorporate the chirp observation, the H/V ratio 395 measures, and other available data like the normalized compliance measures from the 396 Martian pressure drops (e.g. Kenda et al., 2020; Onodera, 2022). 397

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5.2 Higher-mode guided infrasound from the atmospheric model

The S0793a seismic recording includes a chirp signal in the time domain (Figure 7a). 399 However, in opposition to the S0986c and S0981c group velocity measurement, which yields 400 a single monotonous trend (Figure 3c and S1b), the measurement of the S0793a chirp 401 provides two trends (Figure 7b): a horizontal one from 1 to 2 Hz at around 251 m/s, and 402 a sloping one with decreasing velocity, from about 1.2 Hz to 2.3 Hz. The horizontal trend 403 may correspond to an infrasound propagating directly from the impact and requires fur-404 ther investigation. It is ambiguous to attribute the sloping trend to a guided infrasound, 405 since the bandwidth of the trend is short and the trend is not as continuous as the ones 406 of S0981c and S0986c (Figure S1b and S1c). In the rest of this subsection, we present 407 that the sloping trend can be explained by the higher-mode guided infrasound, while we 408 also recognize that there could be other interpretations for the trend like the scattered 409 infrasound (i.e. echoes, Garcia et al., 2022). 410

We compute the fundamental- and 1st-higher-mode group velocities and the eigenfunctions of this guided infrasound by applying our computation (Section 2) to the corresponding infrasound velocity model (Figure 7c). The synthetic fundamental-mode group



Figure 7. (a) The S0793a chirp bandpass filtered between 0.5 and 8 Hz. (b) Comparison of the group-velocity measurement from the chirp (gray) to the synthetic group velocity of the fundamental- and 1st-higher mode. These modes are from a 1D layered model modified from the MCD model (c, Table S1). We also compute the eigenfunctions corresponding to these modes and normalize each eigenfunction by its maximum real value (d and e).

velocity increases with increasing frequency, opposite of the measured group velocity (black 414 curve in Figure 7b). The fundamental-mode eigenfunctions are complex valued, instead 415 of real valued as in S0986c (Section 3b). The real parts of the eigenfunctions are close 416 to zero on the ground surface and increase from the surface to the 1500-m altitude (Fig-417 ure 7d). This means that this fundamental-mode guided infrasound possesses smaller 418 amplitude on the ground surface than at 1500 m altitude. The imaginary parts of the 419 eigenfunctions are large near the ground surface (Figure 7e) and represent energy leak-420 age of the guided infrasound to the top halfspace (e.g. Press & Harkrider, 1962; Radovich 421 & De Bremaecker, 1974). Thus this fundamental mode possesses weak pressure on the 422 ground surface. 423

The 1st-higher-mode guided infrasound of the S0793a atmosphere model possesses a stronger pressure than the fundamental-mode on the ground surface (Figure S1d). We notice that the 1st-higher-mode group velocity agrees with the ground-velocity measurement (the sloping trend in Figure 7b). Furthermore, the real part of the 1st-higher-mode eigenfunctions presents a maximum absolute value on the ground surface, while the imaginary part is close to zero on the ground surface compared to the fundamental-mode. Therefore, the 1st-higher-mode guided infrasound could generate the recorded S0793a chirp.

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5.3 The free surface boundary condition

⁴³² On the ground surface, the vertical particle velocity (v_z) in the atmosphere is equal ⁴³³ to the vertical ground velocity (u_z) . This yields:

$$v_z(z=0) = -u_z(z=0),$$
(23)

where the minus sign is due to different conversion of the positive z-axis direction in atmosphere (altitude) and the subsurface (depth). The formula above and Equation 4 lead to

$$\partial_z p(z=0) = \rho(\partial_t + w_x \partial_x) u_z(z=0), \tag{24}$$

where ρ is the air density. We rewrite this equation as

$$\partial_z P(z=0) = -i\rho(\omega - w_x k) \frac{U_z(z=0)}{T_{zz}(z=0)} P(z=0),$$
(25a)

$$= -i\rho(\omega - w_x k)C_z P(z=0).$$
(25b)

The expected value for C_z on Mars is around $10^{-5}m/s/Pa$ and ρ is about $0.02kg/m^3$. 445 Thus, between 0.5 and 3 Hz, $\partial_z P(z=0)$ is on the order of 10^{-5} of P(z=0). We can 446 conclude that the guided-infrasound atmospheric pressure is almost constant near the 447 ground surface and thus $v_z \approx 0$ (Equation 4). This justifies the rigid ground-surface 448 boundary condition used in our derivation of guided infrasound (Equation 7). Our bench-449 mark (Appendix B) also validates that our modelling result agrees well with the numer-450 ical simulation where v_z is continuous on the ground surface, the atmosphere-solid-earth 451 boundary. 452

We notice that the continuous- v_z boundary condition is necessary for modelling the coupled normal mode between a planet atmosphere and the solid planet (e.g. Watada, 1995; Lognonné et al., 1998; Tanimoto, 2001). Thus in order to be able to model the coupled mode, we will incorporate this boundary condition into our modelling in future.

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5.4 Potential improvement and future work

In our forward modelling, we assume the boundary between the atmosphere and the ground to be flat. However, the ground surface topography affects the compliance (e.g. Bishop et al., 2021) by altering the guided infrasound horizontal wavenumber relative to the ground surface. To incorporate the topography into the compliance computation, we can compute the spatial wavenumber of the topography and combine the wavenumber with the one of guided infrasound, similar to the microseism studies which consider ocean waves coupling with topographic seafloors (e.g. Ardhuin et al., 2015).

Since our forward modelling is fast in computation, one can adopt this modelling 465 to perform a Markov-chain Monte Carlo inversion of the atmospheric and subsurface pa-466 rameters from the chirp signals. A Markov-chain Monte Carlo inversion explores differ-467 ent parameter combinations (e.g. Tarantola, 2005). As we demonstrate the trade-off be-468 tween the shear-wave velocity and layer thickness in our three-layer subsurface model 469 (Section 4), we expect more parameter trade-offs if the subsurface model possesses more 470 than three layers. We also expect a trade-off between the atmospheric and subsurface 471 472 parameters, since the compliance computation depends on the guided-infrasound phase velocity from the atmospheric model. Thus the inversion could aid us to assess these trade-473 offs between both the atmospheric (like infrasound velocity) and the subsurface (e.g. Vs 474 and layer thickness) parameters. 475

476 6 Conclusion

We analytically model chirp, the seismic waveform due to the coupling between guided infrasound and the ground. We theoretically demonstrate the guided-infrasound propagation in a 1D atmospheric model and compute the guided-infrasound phase and group velocities. Our group velocities match well with the measures from the S0981c and S098c chirp observation on Mars. We convert the guided infrasound into a chirp through compliance of a three-layer subsurface velocity model. We validate our modelling through a benchmark.

By applying our modelling to the Martian atmospheric model, we model synthetic 484 chirps to fit the real chirp recordings of S0981c and S0986c. Through the waveform fit-485 ting, we achieve a three-layer Martian subsurface velocity model, where the coarse re-486 golith is 40-m thick. We also apply our modelling to examine the velocity models from 487 the InSight ambient-seismic-vibration H/V ratio observation and present that these mod-488 els explain a part of the chirp recordings but do not provide a good fitting as our three-489 layer model. Therefore we need to incorporate all the available observations to constrain 490 the Martian subsurface structure estimation. 491

⁴⁹² 7 Open Research and Data Availability Statement

The Martian topography data are from the NASA PDS Geosciences Node (Neumann et al., 2003) The InSight seismic waveform data are available from the IPGP Datacenter, IRIS-DMC and the NASA PDS (InSight Mars SEIS Data Service, 2019a, 2019b). The Martian atmospheric parameters are from MCD (Millour et al., 2018). The codes for computation of the guided infrasound are available in Xu (2022).

498 Appendix A Guided infrasound on Earth

We present a terrestrial example of chirp, where the infrasound source is the 2017-499 12-12 Baumgarten gas hub explosion in Austria. This event generates both seismic waves 500 and infrasound. These infrasound couples to the ground and are recorded by local seis-501 mic stations (Schneider et al., 2018). From these stations, we choose one from AlpAr-502 ray (Hetényi et al., 2018), A333A (Figure A1), at the northeast of the explosion. The 503 A333A vertical-component recording presents a chirp (Figure A1b), from which we mea-504 sure the group velocity (Figure A1d). Our group-velocity measurement method is de-505 tailed in Panning et al. (2015) and Drilleau et al. (2020). We choose an atmospheric pro-506 file used in Schneider et al. (2018) and follow the computation in Section 2 to compute 507 the synthetic group velocity. The difference between the measured and synthetic group 508 velocity indicates that we can improve the Earth low-altitude (<3000 m) atmospheric 509 model using the guided infrasound. 510

511 Appendix B Benchmark

We benchmark our modelling against a numerical simulation software, SPECFEM2D-512 DG (Martire et al., 2020). SPECFEM2D-DG can model acoustic and seismic waves in 513 a coupled solid-fluid system. Garcia et al. (2022) utilize this software to simulate the seis-514 mic recording at InSight location due to the S0793a, S0981c, and S0986c impacts. We 515 choose the S0981c simulation result in this benchmark. Garcia et al. (2022) use the S0981c 516 atmospheric model from MCD (Millour et al., 2018) and a four-layer subsurface model 517 (Table B1). Garcia et al. (2022) set the pressure and seismic receivers 246 km away from 518 the source and the seismic receiver at 5 m under the ground surface. We use the same 519 models and the same receiver setting. We compare our modelling result to the one from 520 Garcia et al. (2022): the group velocity (Figure B1a), the compliance (Figure B1b), and 521 the pressure and seismic waveforms (Figure B2). Those match well in the frequency do-522 main or the time domain. Note that in the seismic waveform comparison, since SPECFEM2D-523 DG is for the 2D space, instead of the 3D, we have to modify Equation 20 and 20 by re-524 moving the 3D cylindrical wave term: 525

$$u_z = \mathscr{F}^{-1}\left[S(\omega)\exp\left(-ikx - ax\right)\frac{P^2(\omega, 0)}{\int P^2(\omega, z)dz}C_z(\omega)\right],\tag{B1}$$

$$u_x = \mathscr{F}^{-1} \left[S(\omega) \exp\left(-ikx - ax\right) \frac{P^2(\omega, 0)}{\int P^2(\omega, z) dz} C_x(\omega) \right].$$
 (B2)



Figure A1. Illustration of the A333A chirp (a,b) and computation of the group velocity (c,d). We bandpass filter the A333A vertical-component velocity recording between 0.5 and 5 Hz (a) and in multiple narrow bands (b). We measure group velocity from the recording (a) and pick the probability maximum at each frequency as the group velocity (blue line in d). Based on the ECMWF profile used in Schneider et al. (2018), we plot the effective acoustic-wave velocity profile (red dashed line in c) and the 1D layered model (black line in c). From the 1D model, we compute the synthetic group velocity (red line in d). We convert the synthetic and measured group velocities at the narrow bands to the corresponding arrival times (red and blue bars in b).

Layer number	$V_P(m/s)$	$V_S(m/s)$	Density (kg/m^3)	Thickness (m)
1	744	398	1800	100
2	3800	1850	2304	9900
3	4500	2800	2570	14000
4	6224	3753	2863	∞

Table B1. The subsurface velocity model used in (Garcia et al., 2022). Note that we only usethis model in the benchmark section.



Figure B1. The comparison of the group velocity and compliance from our analytical approach to SPECFEM2D-DG. The group velocity measurement and compliance values from SPECFEM2D-DG are the gray background (a) and the empty circles (b), respectively. The estimates from our analytical approach are in the curves (a,b).

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Figure B2. The waveform comparison of the atmospheric pressure, vertical velocity, and horizontal velocity from our analytical approach to SPECFEM2D-DG. The waveforms are all bandpass filtered between 0.5 and 2 Hz. We normalize our waveforms by the maximum value of the pressure from SPECFEM2D-DG.

542 **References**

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- Aki, K., & Richards, P. G. (2002). *Quantitative seismology*.
- Ardhuin, F., Gualtieri, L., & Stutzmann, E. (2015). How ocean waves rock the
 Earth: Two mechanisms explain microseisms with periods 3 to 300 s. *Geophys- ical Research Letters*, 42(3), 765–772.
- Assink, J. D. (2012). Infrasound as upper atmospheric monitor. *Ph. D. Thesis*.
- Banerdt, W. B., Smrekar, S. E., Banfield, D., Giardini, D., Golombek, M., Johnson,
 C. L., ... others (2020). Initial results from the InSight mission on Mars.
 Nature Geoscience, 13(3), 183–189.
- Banfield, D., Rodriguez-Manfredi, J., Russell, C., Rowe, K., Leneman, D., Lai, H.,
 ... others (2019). InSight auxiliary payload sensor suite (APSS). Space
 Science Reviews, 215(1), 1–33.
- Bass, H. E., & Chambers, J. P. (2001). Absorption of sound in the Martian atmosphere. The Journal of the Acoustical Society of America, 109(6), 3069–3071.
 - Ben-Menahem, A., & Singh, S. J. (2012). Seismic waves and sources. Springer Science & Business Media.
- Bishop, J. W., Fee, D., Modrak, R., Tape, C., & Kim, K. (2021). Spectral element
 modeling of acoustic to seismic coupling over topography. Journal of Geophysical Research: Solid Earth, e2021JB023142.
- Chakravarthy, G. V. R. (2008). Love Wave Propagation in Viscoelastic Media. Boise
 State University Theses and Dissertations.
 - Clinton, J. F., Ceylan, S., van Driel, M., Giardini, D., Stähler, S. C., Böse, M., ... others (2021). The Marsquake catalogue from InSight, sols 0–478. *Physics of* the Earth and Planetary Interiors, 310, 106595.
 - Drilleau, M., Beucler, E., Lognonné, P., Panning, M. P., Knapmeyer-Endrun, B., Banerdt, W. B., ... others (2020). MSS/1: Single-station and single-event marsquake inversion. *Earth and Space Science*, 7(12), e2020EA001118.
 - Edwards, W. N., Eaton, D. W., & Brown, P. G. (2008). Seismic observations of meteors: Coupling theory and observations. *Reviews of Geophysics*, 46(4).
- ⁵⁷¹ Ewing, W. M., Jardetzky, W. S., Press, F., & Beiser, A. (1957). Elastic waves in
 ⁵⁷² layered media.
- Garcia, R. F., Brissaud, Q., Rolland, L., Martin, R., Komatitsch, D., Spiga, A., ...
 Banerdt, B. (2017). Finite-difference modeling of acoustic and gravity wave propagation in Mars atmosphere: application to infrasounds emitted by meteor impacts. Space Science Reviews, 211(1), 547–570.
- Garcia, R. F., Daubar, I. J., Beucler, É., Posiolova, L., Collins, G. S., Lognonné,
 P., ... others (2022). Seismological location and orbital imaging of
 newly formed craters on Mars. Nature Geosciences, online. doi: 10.1038/
 s41561-022-01014-0
- Garcia, R. F., Kenda, B., Kawamura, T., Spiga, A., Murdoch, N., Lognonné, P. H.,
 ... others (2020). Pressure effects on the SEIS-InSight instrument, improvement of seismic records, and characterization of long period atmospheric waves from ground displacements. Journal of Geophysical Research: Planets, 125(7),
 e2019JE006278.
- Gardner, G., Gardner, L., & Gregory, A. (1974). Formation velocity and den sity—The diagnostic basics for stratigraphic traps. *Geophysics*, 39(6), 770–
 780.
- Giardini, D., Lognonné, P., Banerdt, W. B., Pike, W. T., Christensen, U., Ceylan,
 S., ... others (2020). The seismicity of Mars. Nature Geoscience, 13(3),
 205-212.
- Gibbons, S. J., Ringdal, F., & Kværna, T. (2007). Joint seismic-infrasonic process ing of recordings from a repeating source of atmospheric explosions. The Jour nal of the Acoustical Society of America, 122(5), EL158-EL164.
- ⁵⁹⁵ Grott, M., Spohn, T., Knollenberg, J., Krause, C., Hudson, T. L., Piqueux, S., ...
- others (2021). Thermal conductivity of the Martian soil at the InSight landing

597	site from HP3 active heating experiments. Journal of Geophysical Research: $Plamete_{1,2} = 126(7)$, p2021 JE006861
598	Harden D C (1064) Theoretical and observed acoustic gravity waves from
599	Harkfider, D. G. (1904). Theoretical and observed acoustic-gravity waves from $G_{0}(24)$
600	explosive sources in the atmosphere. <i>Journal of Geophysical Research</i> , 09(24),
601	3295 = 3521.
602	Herrin, E. I., Kim, I. S., & Stump, B. W. (2006). Evidence for an infrasound $(1 - 1)$
603	waveguide. Geophysical research letters, 33(7).
604	Hetenyi, G., Molinari, I., Clinton, J., Bokelmann, G., Bondar, I., Crawford, W. C.,
605	others (2018). The AlpArray seismic network: a large-scale European $C_{\rm error}$ in some horizon $20(5)$ 1000
606	experiment to image the Alpine orogen. Surveys in geophysics, 39(5), 1009–
607	1055. Habiran M. Halla, M. Sahmalahash, C. Stählan, S. Fähl D. Ciandini, D. ath
608	(2021) The shallow structure of Mars at the InSight landing site from
609	ers (2021). The shahow structure of Mars at the hisight failung site from inversion of ambient vibrations. Nature communications $10(1)$, 1, 12
610	Inversion of ambient vibrations. Nature communications, $12(1)$, 1–13.
611	valcanic activity using correlation patterns between infrasound and ground
612	wotion Coophysical Research Latters $20(4)$
613	In Sight Mars SFIS Data Service (2010a) Data Service In Sight SFIS Data Bundle
614	PDS Geosciences (GEO) Node. doi: 10.17189/1517570
616	InSight Mars SEIS Data Service. (2019b). SEIS raw data. InSight mission. IPGP.
617	JPL, CNES, ETHZ, ICL, MPS, ISAE-Supaero, LPG, MFSC. doi: https://doi
618	.org/10.18715/SEIS.INSIGHT.XB
619	Kenda, B., Drilleau, M., Garcia, R. F., Kawamura, T., Murdoch, N., Compaire, N.,
620	others (2020). Subsurface structure at the InSight landing site from com-
621	pliance measurements by seismic and meteorological experiments. Journal of
622	Geophysical Research: Planets, 125(6), e2020JE006387.
623	Kenda, B., Lognonné, P., Spiga, A., Kawamura, T., Kedar, S., Banerdt, W. B.,
624	Golombek, M. (2017). Modeling of ground deformation and shallow sur-
625	face waves generated by Martian dust devils and perspectives for near-surface
626	structure inversion. Space Science Reviews, $211(1)$, $501-524$.
627	Landau, L. D., & Lifshitz, E. M. (2013). Fluid mechanics: Landau and lifshitz:
628	Course of theoretical physics, volume 6 (Vol. 6). Elsevier.
629	Langston, C. A. (2004). Seismic ground motions from a bolide shock wave. Journal of Geophysical Research: Solid Earth 100(B12)
631	Lognonné P. Banerdt W. Pike W. Giardini D. Christensen II. Garcia B. F.
622	others (2020) Constraints on the shallow elastic and anelastic structure of
633	Mars from InSight seismic data Nature Geoscience 13(3) 213–220
624	Lognonné P Banerdt W B Giardini D Pike W T Christensen U Laudet
635	P others (2019) SEIS Insight's seismic experiment for internal structure
636	of Mars. Space Science Reviews, 215(1), 1–170.
637	Lognonné, P., Clévédé, E., & Kanamori, H. (1998). Computation of seismograms
638	and atmospheric oscillations by normal-mode summation for a spherical earth
639	model with realistic atmosphere. <i>Geophysical Journal International</i> , 135(2).
640	388–406.
641	Lorenz, R. D., Kedar, S., Murdoch, N., Lognonné, P., Kawamura, T., Mimoun, D.,
642	& Bruce Banerdt, W. (2015). Seismometer detection of dust devil vortices by
643	ground tilt. Bulletin of the Seismological Society of America, 105(6), 3015-
644	3023.
645	Martire, L., Garcia, R. F., Rolland, L., Spiga, A., Lognonné, P. H., Banfield, D.,
646	Martin, R. (2020). Martian infrasound: Numerical modeling and anal-
647	ysis of InSight's data. Journal of Geophysical Research: Planets, 125(6),
648	e2020JE006376.
649	Maupin, V. (2017). 3-D sensitivity kernels of the Rayleigh wave ellipticity. Geophys-
650	ical Journal International, 211(1), 107–119.

Millour, E., Forget, F., Spiga, A., Vals, M., Zakharov, V., & Montabone, L. (2018). 651

652	Mars Climate Database. From Mars Express to ExoMars, 68.
653	Morgan, P., Grott, M., Knapmeyer-Endrun, B., Golombek, M., Delage, P.,
654	Lognonné, P., others (2018). A pre-landing assessment of regolith proper-
655	ties at the InSight landing site. Space Science Reviews, $214(6)$, 1–47.
656	Negraru, P. T., & Herrin, E. T. (2009). On infrasound waveguides and dispersion.
657	Seismological Research Letters, $80(4)$, $565-571$.
658	Neumann, G. A., Abshire, J. B., Aharonson, O., Garvin, J. B., Sun, X., & Zuber,
659	M. T. (2003). Mars Orbiter Laser Altimeter pulse width measurements and
660	footprint-scale roughness. Geophysical research letters, $30(11)$.
661	Nijs, L., & Wapenaar, C. (1990). The influence of wind and temperature gradients
662	on sound propagation, calculated with the two-way wave equation. The Jour-
663	nal of the Acoustical Society of America, 87(5), 1987–1998.
664	Nijs, L., & Wapenaar, C. (1992). Reply to: "Comments on the influence of wind
665	and temperature gradients on sound propagation calculated with the two-way
666	wave equation" [J. Acoust. Soc. Am. 9 1, 498–500 (1992)]. The Journal of the
667	Acoustical Society of America, $91(1)$, $501-504$.
668	Onodera, K. (2022). Subsurface structure of the Moon and Mars deduced from 3D
669	seismic wave propagation simulation and analysis of Apollo and InSight seismic
670	data. Doctoral dissertation of The Graduate University for Advanced Studies,
671	SOKENDAI and Université de Paris Cité.
672	Panning, M. P., Beucler, É., Drilleau, M., Mocquet, A., Lognonné, P., & Banerdt,
673	W. B. (2015). Verifying single-station seismic approaches using Earth-based
674	data: Preparation for data return from the InSight mission to Mars. <i>Icarus</i> ,
675	248, 230-242.
676	Pekeris, C. (1948). The propagation of a pulse in the atmosphere. Part II. Physical
677	Review, 73(2), 145.
678	Pierce, A. D. (1990). Wave equation for sound in fluids with unsteady inhomo-
679	geneous flow. The Journal of the Acoustical Society of America, 87(6), 2292–
680	2299.
681	Press, F., & Harkrider, D. (1962). Propagation of acoustic-gravity waves in the at-
682	mosphere. Journal of Geophysical Research, 67(10), 3889–3908.
683	Radovich, B., & De Bremaecker, J. C. (1974). Body waves as normal and leaking
684	modes—leaking modes of Love waves. Bulletin of the Seismological Society of
685	America, 64(2), 301–306.
686	Schneider, F. M., Fuchs, F., Kolínskỳ, P., Caffagni, E., Serafin, S., Dorninger, M.,
687	others (2018). Seismo-acoustic signals of the Baumgarten (Austria) gas explo-
688	sion detected by the AlpArray seismic network. Earth and Planetary Science
689	Letters, 502, 104–114.
690	Smith, D. E., Zuber, M. T., Frey, H. V., Garvin, J. B., Head, J. W., Muhleman,
691	D. O., others (2001). Mars Orbiter Laser Altimeter: Experiment sum-
692	mary after the first year of global mapping of Mars. Journal of Geophysical
693	Research: Planets, 106(E10), 23689–23722.
694	Sorrells, G. G. (1971). A preliminary investigation into the relationship between
695	long-period seismic noise and local fluctuations in the atmospheric pressure
696	field. Geophysical Journal International, 26(1-4), 71–82.
697	Sorrells, G. G., McDonald, J. A., Der, Z., & Herrin, E. (1971). Earth motion caused
698	by local atmospheric pressure changes. <i>Geophysical Journal International</i> ,
699	26(1-4), 83-98.
700	Stutzmann, É., Schimmel, M., Lognonné, P., Horleston, A., Ceylan, S., van Driel,
701	M., others (2021). The polarization of ambient noise on Mars. Journal of
702	Geophysical Research: Planets, 126(1), e2020JE006545.
703	Tanimoto, T. (2001). Continuous free oscillations: atmosphere-solid earth coupling.
704	Annual Review of Earth and Planetary Sciences, 29(1), 563–584.
705	Tanimoto, T., & Wang, J. (2019). Theory for deriving shallow elasticity structure
706	from colocated seismic and pressure data. Journal of Geophysical Research:

707	Solid Earth, 124(6), 5811–5835.
708	Tarantola, A. (2005). Inverse problem theory and methods for model parameter esti-
709	mation (Vol. 89). siam.
710	Warner, N., Golombek, M., Ansan, V., Marteau, E., Williams, N., Grant, J.,
711	others (2022). In Situ and Orbital Stratigraphic Characterization of the
712	InSight Landing Site–A Type Example of a Regolith-Covered Lava Plain on
713	Mars. Journal of Geophysical Research: Planets, e2022JE007232.
714	Warner, N., Golombek, M., Sweeney, J., Fergason, R., Kirk, R., & Schwartz, C.
715	(2017). Near surface stratigraphy and regolith production in southwestern
716	elysium planitia, mars: implications for hesperian-amazonian terrains and the
717	insight lander mission. Space Science Reviews, 211(1), 147–190.
718	Watada, S. (1995). Part I. Near-source acoustic coupling between the atmosphere
719	and the solid earth during volcanic eruptions. Part II. Nearfield normal mode
720	amplitude anomalies of the Landers earthquake. Doctoral dissertation of
721	California Institute of Technology. doi: 10.7907/JSE5-G397
722	Waxler, R. (2002). A vertical eigenfunction expansion for the propagation of sound
723	in a downward-refracting atmosphere over a complex impedance plane. The
724	Journal of the Acoustical Society of America, 112(6), 2540–2552.
725	Waxler, R. (2004). Modal expansions for sound propagation in the nocturnal
726	boundary layer. The Journal of the Acoustical Society of America, $115(4)$,
727	1437 - 1448.
728	Xu, Z. (2022). ZongboXu/HFGI: v1.0.0 (Version v1.0.0). [Software] Zenodo. doi:
729	https://doi.org/10.5281/zenodo.7079346